

456/1
MATHEMATICS
PAPER 1
July/August 2019
2½ hours



WAKISSHA JOINT MOCK EXAMINATIONS

Uganda Certificate of Education

MATHEMATICS

Paper 1

2 hours 30 minutes

INSTRUCTIONS TO CANDIDATES:

- ☒ Answer *all* questions in section A and any *five* questions from section B.
- ☒ Any additional question(s) answered will not be marked.
- ☒ All necessary calculations *must* be done in the same answer booklet/sheets provided, with the rest of the answers. Therefore no paper should be given for rough work.
- ☒ Graph paper is provided.
- ☒ Silent non-programmable scientific calculators and mathematical tables with a list of formulae may be used.

SECTION A (40 marks)

Answer all questions in this section

1. Given that $n \times m = \frac{n+m}{n-m}$, find the value of $(5 \times 3) \times^{-2}$ (04 marks)
2. Factorise completely: $16x^4 - 81$ (04 marks)
3. Figure 1 below shows a circle of centre O.

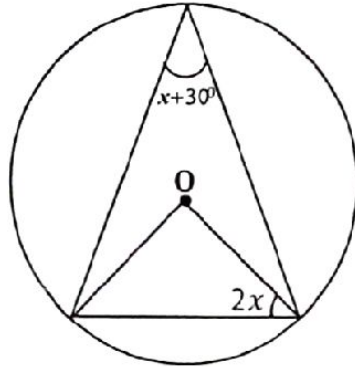


Fig. 1

(04 marks)

Use it to find the value of x .

4. In an election, John got 12,516 votes. This gave him 3,332 more votes than Mary. Together John and Mary received 70% of the total votes. How many people voted? (04 marks)
5. Given that $A = \sqrt{\frac{m-r}{p-mr}}$, make r the subject of the expression (04 marks)
6. Given matrices $X = \begin{pmatrix} 3 & 2 \\ 2 & 4 \end{pmatrix}$ and $Y = \begin{pmatrix} 2 & -1 \\ 3 & 2 \end{pmatrix}$
Find $(X - 2Y)^{-1}$ (04 marks)
7. Solve for x : $\frac{3}{2} - \frac{5x}{3} > 8 + \frac{x}{2}$ (04 marks)
8. Two shirts and a pair of trousers cost Shs. 12,000. One shirt and two pairs of trousers cost Shs. 15,000. Find the cost of a shirt and a pair of trousers. (04 marks)
9. A bag contains **black**, **blue** and **green** balls. The probability of picking a black ball is $\frac{1}{4}$ and that of a blue ball is $\frac{8}{12}$. If the bag contains 84 balls, find the number of green balls in the bag. (04 marks)
10. A ladder 5.3m long is leaning against a vertical wall with its foot 1.7m from the wall. Calculate the angle the ladder makes with the horizontal ground. (04 marks)

SECTION B (60 marks)

Attempt any **five** questions from this section. All questions carry equal marks.

11. Using a ruler, pencil and a pair of compasses only,
- (i) construct a triangle PQR such that $PQ = 8.5\text{cm}$ angle $PQR = 60^\circ$ and angle $QPR = 45^\circ$.
 - (ii) draw a circle to circumscribe the triangle PQR . Measure its radius.
 - (iii) construct a perpendicular from R to meet PQ at N . Measure RN and use it to determine area of triangle PQR . (12 marks)

12. Copy and complete the table below for the graph: $y = 2x^2 + 8x + 3$.

| | | | | | | | | |
|--------|----|-----|----|----|----|---|---|---|
| x | -5 | -4 | -3 | -2 | -1 | 0 | 1 | 2 |
| $2x^2$ | | 32 | | | | | | |
| $8x$ | | -12 | | | | | | |
| 3 | | 3 | | | | | | |
| y | | | | | | | | |

- (b) Use the table completed above to plot a graph of $y = 2x^2 + 8x + 3$. Use your graph to solve the equation:

(i) $2x^2 + 8x - 3 = 0$

(ii) $x^2 + 3x + 1/2 = 0$

(12 marks)

13. The table below shows marks scored by 50 Students in a Chemistry test.

~~32~~ 11 ~~42~~ 51 68 36 33 29 59 32
 22 56 32 78 45 15 47 53 62 46
 37 63 27 47 25 42 25 30 49 23
 66 41 56 35 49 73 58 48 17 53
 58 31 72 40 65 55 39 28 44 64

- (a) Construct a frequency distribution table with equal class interval starting from 10 – 19. (03 marks)
 - (b) Draw a cumulative frequency curve and use it to estimate the;
 - (i) median mark
 - (ii) number of students who scored 35% and above. (07 marks)
 - (c) Calculate the mean mark. (02 marks)
14. Quadrilateral $ABCD$ with coordinates $A(-2, -5)$, $B(4, -3)$, $C(2, 6)$ and $D(-4, 4)$ is transformed by matrix N to form the image $A^1 B^1 C^1 D^1$ with coordinates $A^1(-12, -1)$, $B^1(-2, 15)$, $C^1(14, 0)$ and $D^1(4, 16)$
- (a) Find matrix N .
 - (b) If $A^1 B^1 C^1 D^1$ is then given an enlargement of scale factor +2, centre $(0, 0)$, to produce $A^1 B^1 C^1 D^1$, find the coordinates of A^1 , B^1 , C^1 and D^1 .
 - (c) Find a single matrix of transformation that maps $A^1 B^1 C^1 D^1$ back onto $ABCD$. (12 marks)

15. A plane flies in the *North – East* direction from point *A* to point *B*, a distance of 400km. From point *B*, it flies on a bearing of 145° to point *C*, a distance of 350km.
- (a) Represent this information on a drawing. Use a scale of 1cm: 50km. (06 marks)
- (b) Using your drawing, find the;
 (i) bearing of *A* from *C*.
 (ii) shortest distance between *A* and *C*. (04 marks)
- (c) If the plane has to fly from *C* directly back to *A* at an average speed of 600kmh^{-1} , find the time it takes. (02 marks)

16. L.I.C Investments limited supplied a hotel with *x* executive and *y* ordinary chairs. Given that *y* chairs are at most 10, and the sum of the two types of chairs is more than 15. *y* chairs are also greater than *x* chairs supplied;
- (a) write down three inequalities in terms of *x* and *y* to represent the above information. (03 marks)
- (b) by shading the unwanted region show graphically the feasible region. (06 marks)
- (c) find the maximum number of *x* and *y* types of chairs supplied. (03 marks)

17. *A* and *B* are centres of two circles which touch internally at *P* as shown in figure 2 below. *TP* is 8 cm and it is a common tangent to the two circles.

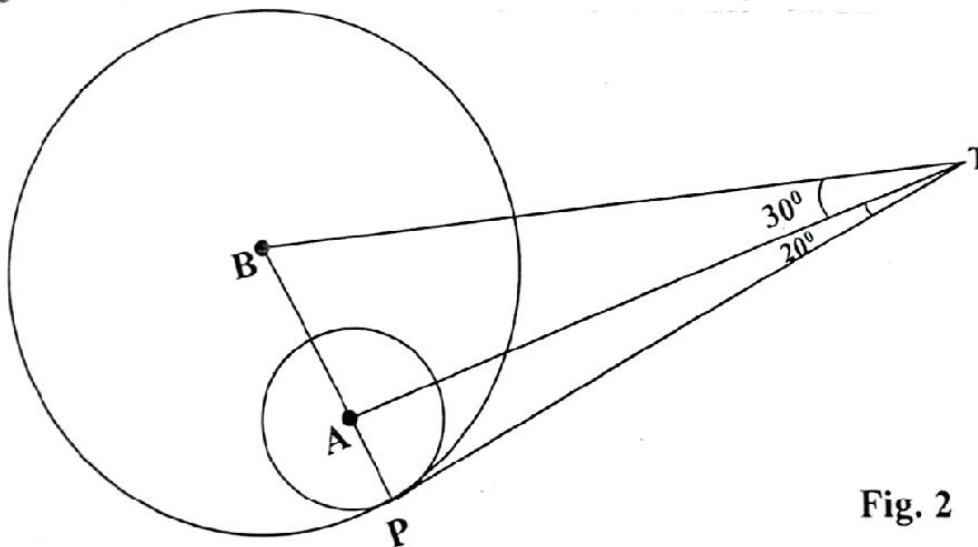


Fig. 2

Calculate the;

- (a) radius of each of the circles. (04 marks)
- (b) distance between the circle centres *A* and *B*. (02 marks)
- (c) area of the larger circle. (03 marks)
- (d) area of triangle *PAT*. (03 marks)

END